

# Graph Convolutional Matrix Completion

Rianne van den Berg      Thomas N. Kipf

Max Welling

Presenter: Yevgeny Tkach

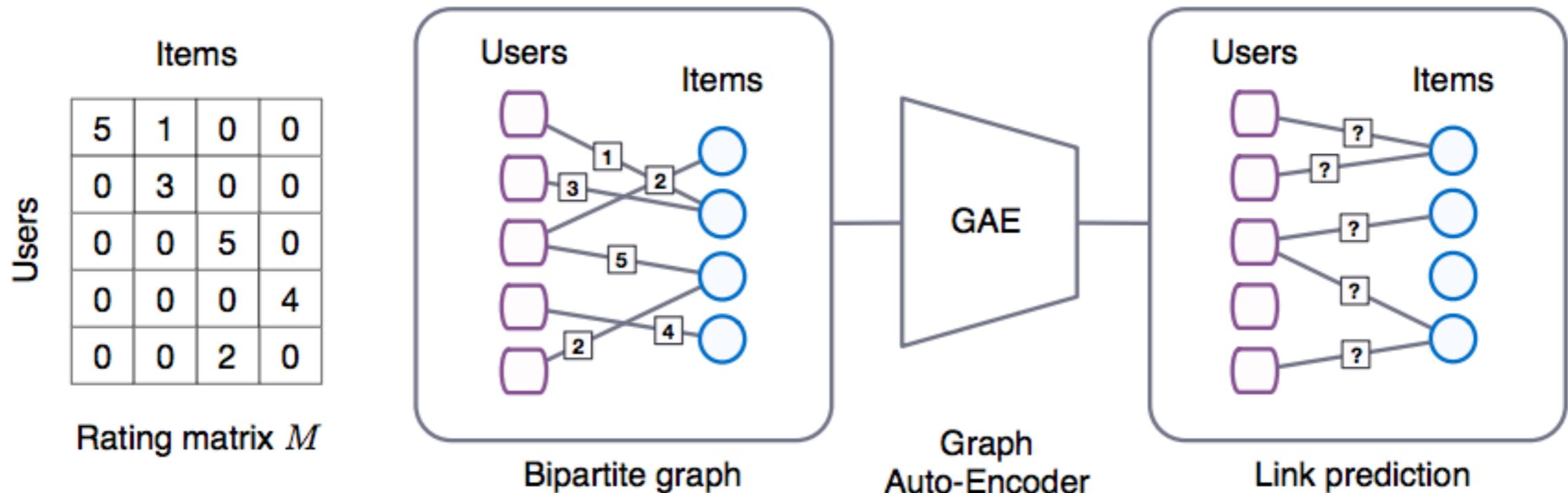
2019 Spring @

<https://qdata.github.io/deep2Read/>

# Executive Summary

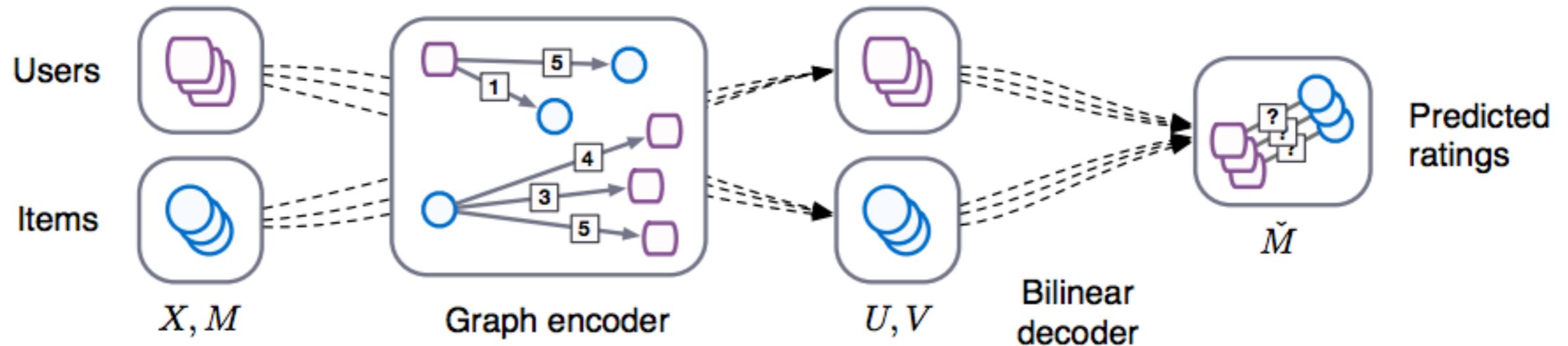
- Matrix completion for recommender systems is reduced to link prediction problem on bipartite user-item graphs with an auto-encoder framework
- This formulation naturally incorporates auxiliary item/user data (node features) in the form of graphs
- Each rating is associated with a different edge type and the predicted score is the expected edge type
- Authors present novel weight sharing strategy for different edge type prediction
- Experiment show competitive performance on standard collaborative filtering (CF) benchmarks and state-of-the-art on CF with user/item graphs

# GCMC



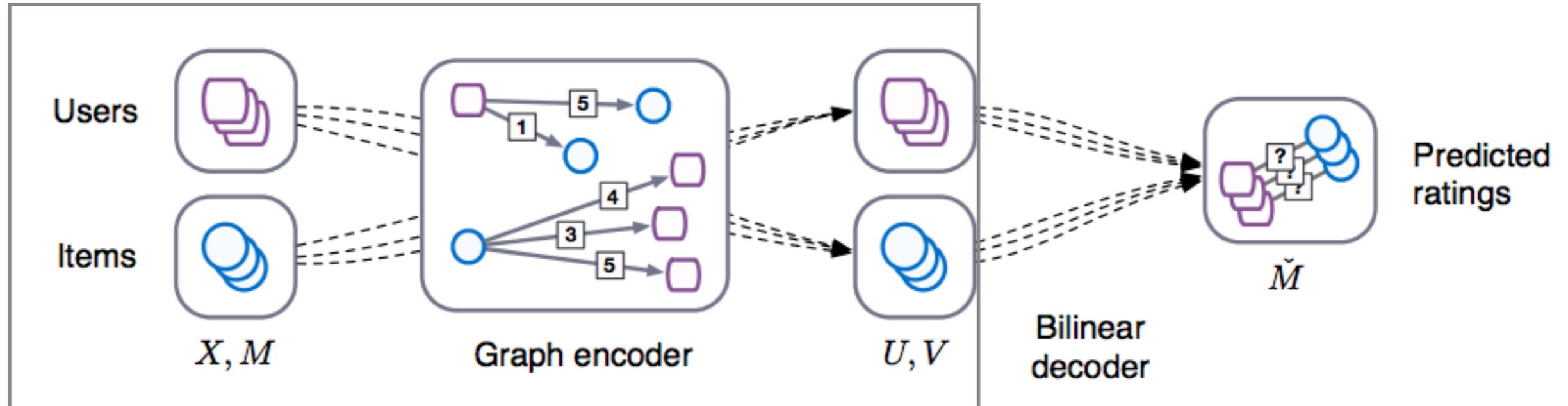
- Rating matrix  $M$  of shape  $N_u \times N_v$ ,  $N_u$  - # of users,  $N_v$  - # of items
- a bipartite  $G=(W,E,R)$  is defined from the matrix such that:
  - $U \cup V = W$  where  $U, V$  - are the user and item nodes, respectively.
  - Edges  $(u_i, r, v_j) \in E$  where  $r$  are ordinal rating levels,  $(u_i, r, v_j) \in E$
  - $R$  adjacency matrices are defined  $M_1, \dots, M_R$  where  $M_r \in \{0, 1\}^{N_u \times N_v}$

# Graph Auto-Encoder



- Here  $X$  is a feature matrix of shape  $N \times D$
- Encoder produces  $[U, V] = f(X, M_1, \dots, M_R)$  where  $U$  and  $V$  are metrics of user and item embeddings respectively of shape  $N_u \times E$  and  $N_v \times E$
- The decoder tries to reconstruct the rating matrix  $\tilde{M} = g(U, V)$  based on the per of user and item embeddings
- $\tilde{M}$  is calculated by the expectation over the rank specific adjacency matrices

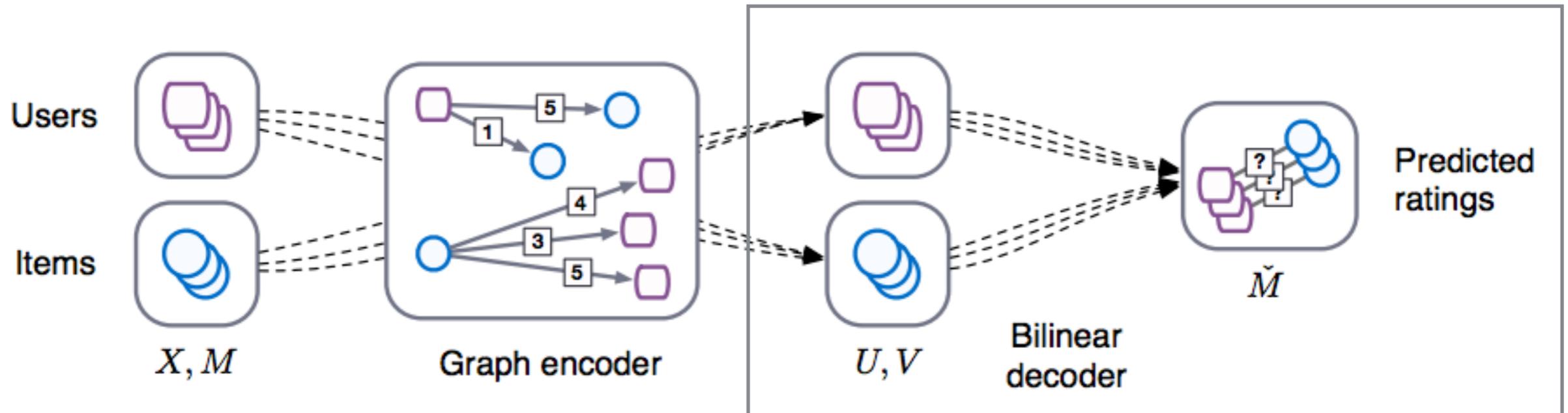
# Graph Convolutional Encoder



- User embeddings:

- edge type specific message from item  $j$  to user  $i$   $\mu_{j \rightarrow i, r} = \frac{1}{c_{ij}} W_r x_j$
- $c_{ij}$  normalization factor  $|\mathcal{N}_i|$  or  $\sqrt{|\mathcal{N}_i| |\mathcal{N}_j|}$
- Weight sharing setup:  $W_r = \sum_{s=1}^r T_s$
- Graph Convolution layer:  $h_i = \sigma \left[ \text{accum} \left( \sum_{j \in \mathcal{N}_{i,1}} \mu_{j \rightarrow i,1}, \dots, \sum_{j \in \mathcal{N}_{i,R}} \mu_{j \rightarrow i,R} \right) \right]$
- Dense layer:  $u_i = \sigma(W h_i)$
- If user info available  $x_i^f$ , then:  $u_i = \sigma(W h_i + W_2^f f_i)$  with  $f_i = \sigma(W_1^f x_i^f + b)$

# Bilinear decoder



- rank prediction:

- $$p(\check{M}_{ij} = r) = \frac{e^{u_i^T Q_r v_j}}{\sum_{s \in R} e^{u_i^T Q_s v_j}}$$
 where:

- $$Q_r = \sum_{s=1}^{n_b} a_{rs} P_s$$
 is a trainable parameter matrix

- Loss function: Negative log likelihood

$$\mathcal{L} = - \sum_{i,j; \Omega_{ij}=1} \sum_{r=1}^R I[r = M_{ij}] \log p(\check{M}_{ij} = r)$$

# Experiments

- **MovieLens 100K** - user-item rating matrix that's accompanied by user and item side information.
- **MovieLens 1M and 10M** - Same as the 100K dataset with more items, users and possible ratings, and without side information. This is the current standard for comparing matrix completion algorithms.
- **Flixster, Douban and YahooMusic** - These datasets include user/item side information in the form of graphs (i.e. connecting user-user and item-item). For GC-MC side information is represented as the relevant row from the side-graph adjacency matrix normalized by the degree.

---

Dataset	Users	Items	Features	Ratings	Density	Rating levels
Flixster	3,000	3,000	Users/Items	26,173	0.0029	0.5, 1, ..., 5
Douban	3,000	3,000	Users	136,891	0.0152	1, 2, ..., 5
YahooMusic	3,000	3,000	Items	5,335	0.0006	1, 2, ..., 100
MovieLens 100K (ML-100K)	943	1,682	Users/Items	100,000	0.0630	1, 2, ..., 5
MovieLens 1M (ML-1M)	6,040	3,706	—	1,000,209	0.0447	1, 2, ..., 5
MovieLens 10M (ML-10M)	69,878	10,677	—	10,000,054	0.0134	0.5, 1, ..., 5

Table 1: Number of users, items and ratings for each of the MovieLens datasets used in our experiments. We further indicate rating density and rating levels.

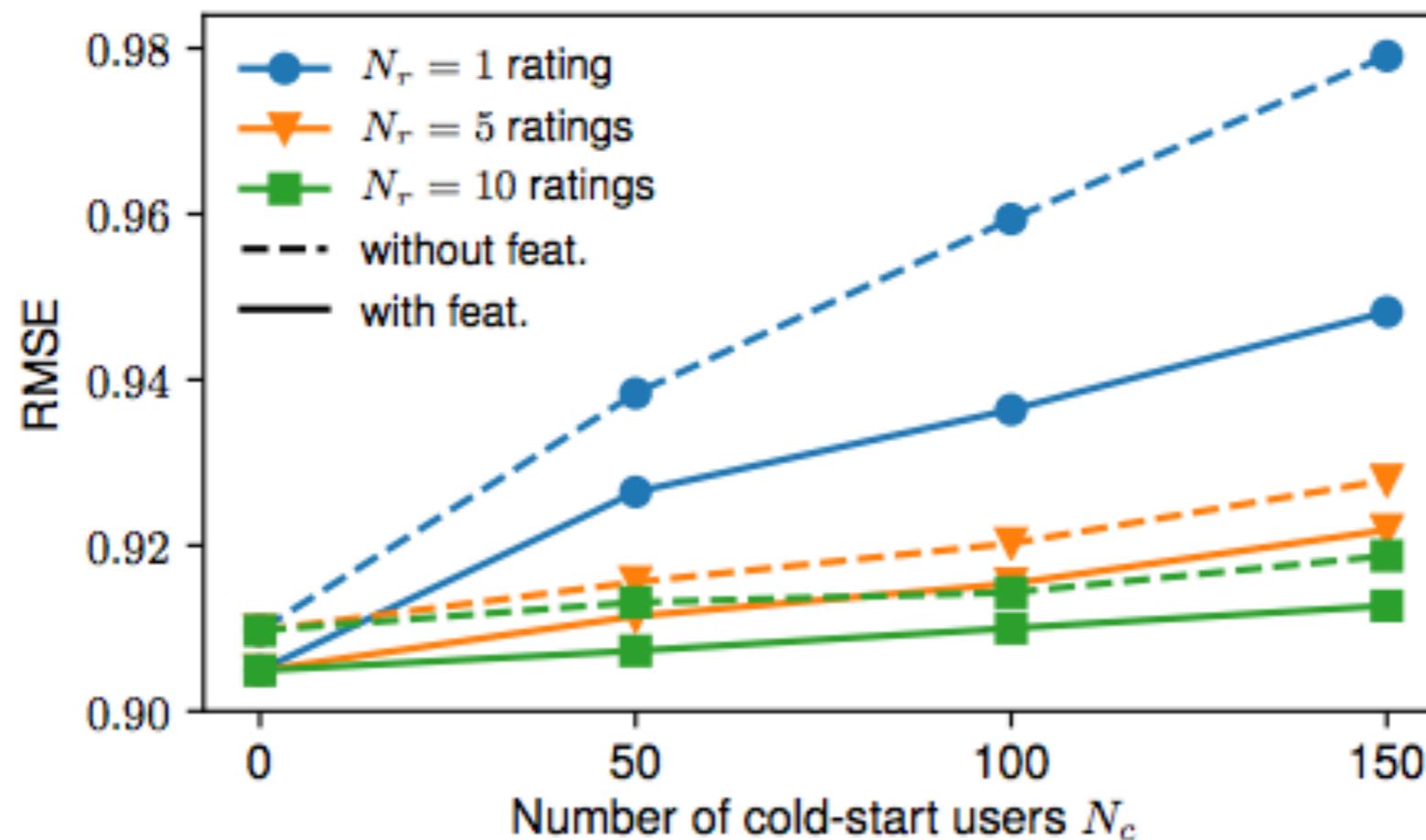
# Experiment results

Model	ML-100K + Feat	Model	ML-1M	ML-10M
MC [3]	0.973	PMF [20]	0.883	–
IMC [11, 31]	1.653	I-RBM [26]	0.854	0.825
GMC [12]	0.996	BiasMF [16]	0.845	0.803
GRALS [25]	0.945	NNMF [7]	0.843	–
sRGCNN [22]	0.929	LLORMA-Local [17]	0.833	0.782
GC-MC (Ours)	0.910	I-AUTOREC [27]	0.831	0.782
GC-MC+Feat	<b>0.905</b>	CF-NADE [32]	<b>0.829</b>	<b>0.771</b>
		GC-MC (Ours)	0.832	0.777

Model	Flixster	Douban	YahooMusic
GRALS	1.313/1.245	0.833	38.0
sRGCNN	1.179/0.926	0.801	22.4
GC-MC	<b>0.941/0.917</b>	<b>0.734</b>	<b>20.5</b>

# Experiment results

- **Cold-start analysis** - The experiment looks at MovieLens100K dataset and tries to verify the added value of side information by masking the available ratings of  $N_c$  users to be no more than  $N_r$ . In the original dataset each user had at least 20 available ratings.



# Discussion

- The authors present a novel interpretation of the matrix completion task as a bipartite graph edge prediction problem.
- This approach outperforms other benchmarks in incorporating auxiliary information about the users and provide almost state of the art results for large matrix completion problems.
- This problem formation is more flexible and allows to incorporate naturally different types of data and structure together.
- The authors offer a simple and clean approach for weight sharing which can be extended to different edges types as well