

# Learning Deep Parsimonious Representations

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## Motivation:

- Advanced Neural Network (NN) needs regularization, which is key to prevent overfitting and improve generalization of the learned classifier.
- No neural network representations to form clusters.
- Not that related to term “Parsimonious Representations”?

## Problem Setting:

- Input: Training set
- Target: Regularized Deep Neural Net considering different clusters (e.g., sample clustering, spatial clustering, channel co-clustering).
- In this talk, I'll focus on sample clustering.

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# Previous Solutions

- Batch Normalization : imposing constrains in the mini-batch
- Dropout : prevent co-adaption
- K-means clustering

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# Contributions

- a new type of regularization that encourages the network representations to form clusters
- This benefits unsupervised learning and zero-shot learning.
- Certain equations in this paper is problematic.

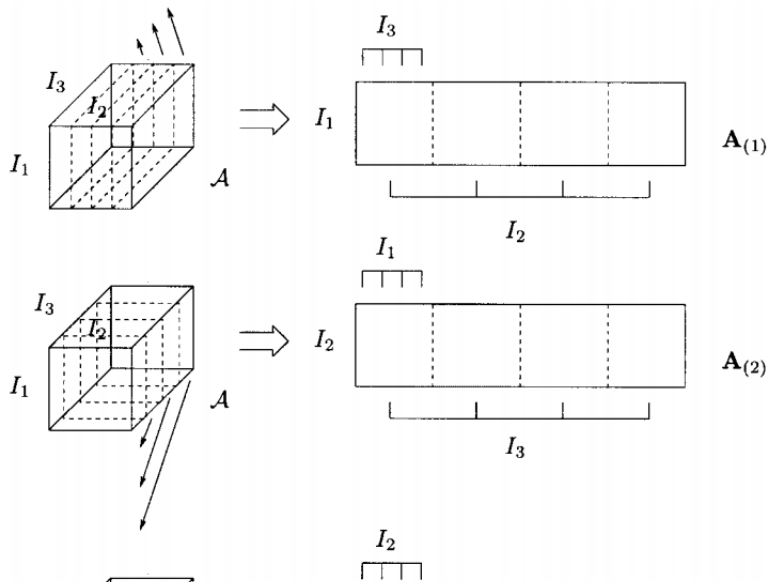


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# Notations

- $[K]: \{1, 2, \dots, K\}$ .
- $\setminus$ : The sets subtraction.
- $\mathbf{Y} \in \mathbb{R}^{I_1 \times I_2 \times \dots \times I_D}$ : An  $n$ -mode vectors of a  $D$ -order tensor.
- $\mathcal{T}\{I_n\} \times \{I_j | j \in [D] \setminus n\}$ : the  $N$ -mode matrix unfolding.

# The $N$ -node matrix unfolding



# The $N$ -node matrix unfolding

A whiteboard example.

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# Problem setting

We assume the representation of one layer within a neural network to be a  $4 - D$  tensor  $\mathbf{Y} \in \mathbb{R}^{N \times C \times H \times W}$ .

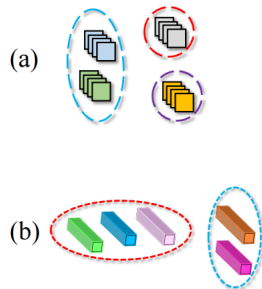
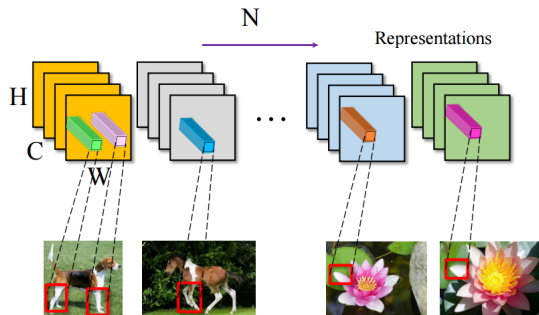
- $N$ : the number of samples within a mini-batch
- $C$ : the number of hidden units in this layer
- $H$ : the height of the output of this layer
- $W$ : the width of the output of this layer

For example,  $H = W = 1$  when this layer is a fully connected layer.

# Calculate $H$ and $W$

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F + 2P)/S + 1$
  - $H_2 = (H_1 - F + 2P)/S + 1$  (i.e. width and height are computed equally by symmetry)
  - $D_2 = K$

# Problem setting

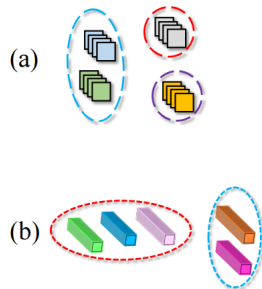
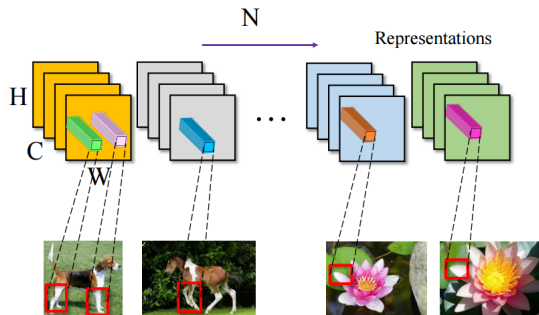




# Problem setting: Clustering in different layers

- Bottom layer representations may focus on low-level visual cues, such as color and edges.
- Top layer features may focus on high-level attributes which have a more semantic meaning.
- See the examples in the figure.

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# Key insight: Regularized formulation

To use the clusters in a certain layer, this paper choose the following formulation:

$$\arg \min \mathcal{L} + \mathcal{R} \quad (1)$$

Where  $\mathcal{L}$  is the loss function and  $\mathcal{R}$  is a regularizer push the clustering structure in a certain layer.

The problem left is the formulation of  $\mathcal{R}$ .

# Key insight: Sample Clustering Regularizer

Suppose  $\mathbf{Y} \in \mathbb{R}^{N \times C \times H \times W}$ , the matrix unfolding of  $\mathbf{Y}$  by the sample dimension is  $\mathcal{T}^{\{N\} \times \{H, W, C\}}(\mathbf{Y}) \in \mathbb{R}^{N \times HWC}$ . Then the regularizer formulate as follows:

$$\mathcal{R}_{\text{sample}}(\mathbf{Y}, \mu) = \frac{1}{2NHC} \sum_{n=1}^N \left\| \mathcal{T}^{\{N\} \times \{H, W, C\}}(\mathbf{Y})_n - \mu_{z_n} \right\|^2 \quad (2)$$

Where  $\mu$  is a matrix size  $K \times HWC$  encoding all the centers with  $K$  the total number of clusters.  $z_n \in [K]$  means which cluster the  $n$ -th sample belongs to.

Clearly, if the  $n$ -th sample belongs to a wrong cluster, the value of this regularizer becomes large.

# Key insight: How to optimize

- In each layer you want to add this sample clustering regularization, you implement a smoothed k-means algorithm
- After you get fixed  $\mu$ , you update weights by backpropagation.

Let  $\mathcal{T}^{\{N\} \times \{H,W,C\}}(\mathbf{Y}) = \mathbf{X}$ . Then the gradient of regularizer equals to:

$$\frac{\partial \mathcal{R}}{\partial \mathbf{X}_n} = \frac{1}{NHC} (\mathbf{X}_n - \mu_n) \quad (3)$$

Different from the paper.

# Experiment Results

The result beats the state-of-art baselines in CIFAR 10 and CIFAR 100.

Dataset	CIFAR10 Train	CIFAR10 Test	CIFAR100 Train	CIFAR100 Test
Caffe	94.87 $\pm$ 0.14	76.32 $\pm$ 0.17	68.01 $\pm$ 0.64	46.21 $\pm$ 0.34
Weight Decay	95.34 $\pm$ 0.27	76.79 $\pm$ 0.31	69.32 $\pm$ 0.51	46.93 $\pm$ 0.42
DeCov	88.78 $\pm$ 0.23	79.72 $\pm$ 0.14	77.92	40.34
Dropout	99.10 $\pm$ 0.17	77.45 $\pm$ 0.21	60.77 $\pm$ 0.47	48.70 $\pm$ 0.38
Sample-Clustering	89.93 $\pm$ 0.19	<b>81.05</b> $\pm$ 0.41	63.60 $\pm$ 0.55	<b>50.50</b> $\pm$ 0.38
Spatial-Clustering	90.50 $\pm$ 0.05	<b>81.02</b> $\pm$ 0.12	64.38 $\pm$ 0.38	<b>50.18</b> $\pm$ 0.49
Channel Co-Clustering	89.26 $\pm$ 0.25	<b>80.65</b> $\pm$ 0.23	63.42 $\pm$ 1.34	<b>49.80</b> $\pm$ 0.25

# Summary

- This paper propose a regularized loss function for the deep neural nets, which enforce the clustering in the NN.
- Some prolems left:
  - Some experiment results don't achieve the state-of-art.
  - Certain equation in the paper is hard to understand.