### Long Range Attention and Visualizing BERT

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#### Transformers for Long Range Dependencies

Visualizing BERT

#### Attention



#### Attention

by *ent270*, *ent223* updated 9:35 am et ,mon march 2 ,2015 (*ent223*) *ent63* went familial for fall at its fashion show in *ent231* on sunday ,dedicating its collection to `` mamma" with nary a pair of `` mom jeans " in sight .*ent164* and *ent21*, who are behind the *ent196* brand , sent models down the runway in decidedly feminine dresses and skirts adorned with roses ,lace and even embroidered doodles by the designers ' own nieces and nephews .many of the looks featured saccharine needlework phrases like `` ilove you ,

X dedicated their fall fashion show to moms

### Self Attention





# Self Attention [7]

$$\alpha_{ij} = \frac{\exp\left(x_i^T x_j\right)}{\sum_{l=1}^n \exp\left(x_i^T x_l\right)}$$
(1)  
$$x_i^{l+1} = \sum_{j=1}^n \alpha_{ij} x_j$$
(2)

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# Self Attention [7]

$$X^{l+1} = \operatorname{Attn}(X^{l}, X^{l}, X^{l})$$
(3)  
 
$$\operatorname{Attn}(Q, K, V) = \operatorname{softmax}\left(\frac{QK^{T}}{\sqrt{d_{k}}}\right) V$$
(4)

 $X^0 = lookupTable(x) + positionEncoding(x)$ 

# Self Attention [7]



# Multi-Head Attention [7]



### Multi-Head Attention



### Restricted Neighbor Attention [7]

Only allow attention to k neighbors

Original

#### Restricted



O(Nk)

### Local Attention [5]



 $O(k^2)$ 

where k is the block size and  $B = \frac{N}{k}$  is the number of blocks 12/44

# Block Self Attention [6]



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#### Local Attention



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# Memory Compressed Attention [5]



Reduce the number of keys and values by using a strided convolution. The number of queries remains unchanged.

 $O(N\frac{N}{k})$ 

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### Memory Compressed

#### Original

#### Memory Compressed

### All Masks



# Area Attention [4]

Put groups of original memory keys (e.g. from individual tokens) into "areas"

- Keys: mean of each area:
- Values: sum of each area



### All Masks





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- Choosing p attention heads, set the attention width to  $\sqrt[p]{N}$
- Reach full connectivity after p attention update steps
- Reduces effective computation to  $O(N\sqrt[p]{N})$



- S<sub>i</sub> denotes the set of indices of the input vectors to which the embedding *i* attends
- ► Factorized self-attention instead has p separate attention heads, where the mth head defines a subset of the indices  $A_i^{(m)} \subset \{j : j \le i\}$  and lets  $S_i = A_i^{(m)}$  where  $|A_i^{(m)}| \propto \sqrt[p]{n}$
- For every j ≤ i pair, we set every A such that i can attend to j through a path of locations with maximum length p + 1. Specifically, if (j, a, b, c, ..., i) is the path of indices, then j ∈ A<sub>a</sub><sup>(1)</sup>, a ∈ A<sub>b</sub><sup>(2)</sup>, b ∈ A<sub>c</sub><sup>(3)</sup> and so forth

### Attention Types



Encoder-Decoder Attention



**Encoder Self-Attention** 



MaskedDecoder Self-Attention

### Music Transformer <sup>[3]</sup>

Relative Attention = Softmax 
$$\left(\frac{QK^{\top} + S^{rel}}{\sqrt{D_h}}\right) V$$
 (5)

- ▶  $S^{rel}$ , an  $L \times L$  dimensional logits matrix which modulates the attention probabilities for each head.
- S<sup>rel</sup> = QR<sup>⊤</sup>, where R is a tensor of shape (L, L, D<sub>h</sub>) containing the embeddings that correspond to the relative distances between all keys and queries.

#### Outline

#### Transformers for Long Range Dependencies

Visualizing BERT

### BERT



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#### Context Embeddings

- Hewitt and Manning (2017) The authors find that after a single self attention step (before the nonlinearity) the square of the distance between context embeddings is roughly proportional to tree distance in the dependency parse.
- This paper seeks to answer why

# Visualizing and Measuring the Geometry of BERT<sup>[2]</sup>

#### Goal: explore BERT's internal representations

- Investigate attention matrices
- Investigate context embeddings in relation to parse trees
- Find semantic representations of BERT embeddings

### Semantics of Attention Matrices

- Attention matrices are built on relations between pairs of words. Do they represent grammar structure between these pairs?
- Formulation: can an attention vector for a pair of words classify a dependency relation?

### Semantics of Attention Matrices

 Train linear model on the model-wide attention vector for pairs of words



- 85.8% accuracy on dependency relation prediction from Penn Treebank
- i.e. syntactic information is encoded in attention vectors

#### Context Embeddings

- After a single self attention step, the square of the distance between context embeddings is roughly proportional to tree distance in the dependency parse tree
- Suggests that BERT embeddings are a good alternative to parse tree embeddings

#### Context Embedding Relationships

"The sale of Southern Optical is a part of the program."

"Factories booked \$236.74 billion in orders in September, nearly the same as the \$236.79 billion in August, the Commerce Department said."





----- Ground truth dependency

---- No ground truth dependency, d<sup>2</sup> < 1.5

#### Distance Between Words of All Relations

- Is the actual difference between embedding distance and the tree distance merely noise, or a more interesting pattern?
- By looking at the average embedding distances of each dependency relation, we can see they vary

### Average Distance Between Words of all Relations



 Suggests that BERT's syntactic representation has an additional quantitative aspect beyond traditional dependency grammar

#### **Contextual Semantics**

- Does BERT actually encode contextual meaning into its representation
  - e.g. does "bark" refer to a tree or a dog

#### Contextual Semantics Visualization Tool

- Input: word
- Retrieves: 1000 sentences from wikipedia containing that word
- Outputs: clusters separating the embeddings of the input word for each sentence

#### Contextual Semantics Visualization Tool



#### Quantitative Semantic Evaluation

- For a given word with n senses, create a nearest-neighbor classifier where each neighbor is the centroid of a given word sense's BERT-base embeddings in the training data.
- To classify a new word we find the closest of these centroids
- State of the art F1 score of 71.1

### Concatenated Similarity Ratio

- If word sense is affected by context, then we should be able to influence context embedding positions by systematically varying their context
- Idea: concatenate sentences of the same word with different semantic meanings

A: "He thereupon *went* to London and spent the winter talking to men of wealth." *went*: to move from one place to another.

B: "He went prone on his stomach, the better to pursue his examination." went: to enter into a specified state.

#### Concatenated Similarity Ratio



Figure 5: Average ratio of similarity to sense A vs. similarity to sense B.

#### References I

- Rewon Child, Scott Gray, Alec Radford, and Ilya Sutskever. Generating long sequences with sparse transformers. arXiv preprint arXiv:1904.10509, 2019.
- [2] Andy Coenen, Emily Reif, Ann Yuan, Been Kim, Adam Pearce, Fernanda Viégas, and Martin Wattenberg. Visualizing and measuring the geometry of bert. arXiv preprint arXiv:1906.02715, 2019.
- [3] Cheng-Zhi Anna Huang, Ashish Vaswani, Jakob Uszkoreit, Noam Shazeer, Curtis Hawthorne, Andrew M Dai, Matthew D Hoffman, and Douglas Eck. An improved relative self-attention mechanism for transformer with application to music generation. arXiv preprint arXiv:1809.04281, 2018.
- [4] Yang Li, Lukasz Kaiser, Samy Bengio, and Si Si. Area attention, 2019.

#### References II

- [5] Peter J Liu, Mohammad Saleh, Etienne Pot, Ben Goodrich, Ryan Sepassi, Lukasz Kaiser, and Noam Shazeer. Generating wikipedia by summarizing long sequences. arXiv preprint arXiv:1801.10198, 2018.
- [6] Tao Shen, Tianyi Zhou, Guodong Long, Jing Jiang, and Chengqi Zhang. Bi-directional block self-attention for fast and memory-efficient sequence modeling. arXiv preprint arXiv:1804.00857, 2018.
- [7] Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. In Advances in neural information processing systems, pages 5998–6008, 2017.