# Beyond Word Importance: Contextual <br> Decomposition to Extract Interactions from LSTMs <br> Presenter: Arshdeep Sekhon <br> https://qdata.github.io/deep2Read 

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## Introduction

- LSTM interpretation model
- extracts information about not only which words contributed to an LSTM's prediction
- also how they were combined in order to yield the final prediction
- mathematically decomposing the LSTM's output, able to disambiguate the contributions made at each step by different parts of the sentence.


## Method: LSTM Decomposition

LSTM equations:

$$
\begin{align*}
o_{t} & =\sigma\left(W_{o} x_{t}+V_{o} h_{t-1}+b_{o}\right)  \tag{1}\\
f_{t} & =\sigma\left(W_{f} x_{t}+V_{f} h_{t-1}+b_{f}\right)  \tag{2}\\
i_{t} & =\sigma\left(W_{i} x_{t}+V_{i} h_{t-1}+b_{i}\right)  \tag{3}\\
g_{t} & =\tanh \left(W_{g} x_{t}+V_{g} h_{t-1}+b_{g}\right)  \tag{4}\\
c_{t} & =f_{t} \odot c_{t-1}+i_{t} \odot g_{t}  \tag{5}\\
h_{t} & =o_{t} \odot \tanh \left(c_{t}\right) \tag{6}
\end{align*}
$$

After processing the full sequence, the final state $h_{T}$ used as input to a linear layer + SoftMax ( multinomial logistic regression), to return a probability distribution $p$ over $C$ classes, with

$$
\begin{equation*}
p_{j}=\operatorname{SoftMax}\left(W h_{T}\right)_{j}=\frac{\exp \left(W_{j} h_{T}\right)}{\sum_{k=1}^{C} \exp \left(W_{k} h_{t}\right)} \tag{7}
\end{equation*}
$$

## Contextual Decomposition

Given an arbitrary phrase $x_{q}, \ldots, x_{r}$, where $1 \leq q \leq r \leq T$, decompose each output $h_{t}$ and cell state $c_{t}$

$$
\begin{align*}
& h_{t}=\beta_{t}+\gamma_{t}  \tag{8}\\
& c_{t}=\beta_{t}^{c}+\gamma_{t}^{c} \tag{9}
\end{align*}
$$

$\beta_{t}$ corresponds to contributions made solely by the given phrase to $h_{t}$, and that $\gamma_{t}$ corresponds to contributions involving, at least in part, elements outside of the phrase. Similarly, $\beta_{t}^{c}$ and $\gamma_{t}^{c}$. final output state $W h_{T}$ :

$$
\begin{equation*}
p=\operatorname{SoftMax}\left(W \beta_{T}+W \gamma_{T}\right) \tag{10}
\end{equation*}
$$

## Contextual Decomposition

$$
\begin{gather*}
i_{t}=\sigma\left(W_{i} x_{t}+V_{i} h_{t-1}+b_{i}\right)  \tag{11}\\
=L_{\sigma}\left(W_{i} x_{t}\right)+L_{\sigma}\left(V_{i} h_{t-1}\right)+L_{\sigma}\left(b_{i}\right)  \tag{12}\\
f_{t} \odot c_{t-1}=  \tag{13}\\
=\left(L_{\sigma}\left(W_{f} x_{t}\right)+L_{\sigma}\left(V_{f} \beta_{t-1}\right)+L_{\sigma}\left(V_{f} \gamma_{t-1}\right)+L_{\sigma}\left(b_{f}\right)\right) \odot\left(\beta_{t-1}^{c}+\right.  \tag{14}\\
= \\
\left.=\left(L_{\sigma}\left(W_{f} x_{t}\right)+L_{\sigma}\left(V_{f} \beta_{t-1}\right)+L_{\sigma}\left(b_{f}\right)\right] \odot \beta_{t-1}^{c}\right)  \tag{15}\\
\\
=\left(L_{\sigma}\left(V_{f} \gamma_{t-1}\right) \odot \beta_{t-1}^{c}+f_{t} \odot \gamma_{t-1}^{c}\right)
\end{gather*}
$$

## Contextual Decomposition

$$
\begin{align*}
i_{t} \odot g_{t}= & {\left[L_{\sigma}\left(W_{i} x_{t}\right)+L_{\sigma}\left(V_{i} \beta_{t-1}\right)+L_{\sigma}\left(V_{i} \gamma_{t-1}\right)+L_{\sigma}\left(b_{i}\right)\right] }  \tag{16}\\
& \odot\left[L_{\tanh }\left(W_{g} x_{t}\right)+L_{\tanh }\left(V_{g} \beta_{t-1}\right)+L_{\tanh }\left(V_{g} \gamma_{t-1}\right)+L_{\tanh }\left(b_{g}\right)\right] \\
= & {\left[L_{\sigma}\left(W_{i} x_{t}\right) \odot\left[L_{\tanh }\left(W_{g} x_{t}\right)+L_{\tanh }\left(V_{g} \beta_{t-1}\right)+L_{\tanh }\left(b_{g}\right)\right]\right.} \\
& +L_{\sigma}\left(V_{i} \beta_{t-1}\right) \odot\left[L_{\tanh }\left(W_{g} x_{t}\right)+L_{\tanh }\left(V_{g} \beta_{t-1}\right)+L_{\tanh }\left(b_{g}\right)\right]  \tag{17}\\
& \left.+L_{\sigma}\left(b_{i}\right) \odot\left[L_{\tanh }\left(W_{g} x_{t}\right)+L_{\mathrm{tanh}}\left(V_{g} \beta_{t-1}\right)\right]\right] \\
& +\left[L_{\sigma}\left(V_{i} \gamma_{t-1}\right) \odot g_{t}+i_{t} \odot L_{\tanh }\left(V_{g} \gamma_{t-1}\right)-L_{\sigma}\left(V_{i} \gamma_{t-1}\right) \odot L_{\tanh }( \right. \\
& \left.+L_{\sigma}\left(b_{i}\right) \odot L_{\tanh }\left(b_{g}\right)\right] \\
= & \beta_{t}^{u}+\gamma_{t}^{u}
\end{align*}
$$

## Cotextual Decomposition

$$
\begin{align*}
& \beta_{t}^{c}=\beta_{t}^{f}+\beta_{t}^{u}  \tag{19}\\
& \gamma_{t}^{c}=\gamma_{t}^{f}+\gamma_{t}^{u} \tag{20}
\end{align*}
$$

$$
\begin{align*}
h_{t} & =o_{t} \odot \tanh \left(c_{t}\right)  \tag{21}\\
& =o_{t} \odot\left[L_{\tanh }\left(\beta_{t}^{c}\right)+L_{\tanh }\left(\gamma_{t}^{c}\right)\right]  \tag{22}\\
& =o_{t} \odot L_{\tanh }\left(\beta_{t}^{c}\right)+o_{t} \odot L_{\tanh }\left(\gamma_{t}^{c}\right)  \tag{23}\\
& =\beta_{t}+\gamma_{t} \tag{24}
\end{align*}
$$

## Linearization of Activation functions

$$
\begin{equation*}
g_{t}=\tanh \left(W_{g} x_{t}+V_{g} h_{t-1}+b_{g}\right) \tag{25}
\end{equation*}
$$

Required:

$$
\begin{gather*}
g_{t}=L_{\tanh }\left(W_{g} x_{t}\right)+L_{\tanh }\left(V_{g} h_{t-1}\right)+L_{\tanh }\left(b_{g}\right)  \tag{26}\\
\tanh \left(\sum y_{i}\right)=\left(\sum L_{\tanh }\left(y_{i}\right)\right) \tag{27}
\end{gather*}
$$

## Linearization of Activation functions

summarization of partial sums as a linearization technique if $y_{1}, \ldots, y_{n}$ are ordered

$$
\begin{equation*}
L_{\tanh }^{\prime}\left(y_{k}\right)=\tanh \left(\sum_{j=1} y_{j}\right)-\tanh \left(\sum_{j=1}^{k-1} y_{j}\right) \tag{28}
\end{equation*}
$$

But no ordering, compute an average over all orderings

$$
\begin{equation*}
L_{\tanh }\left(y_{k}\right)=\frac{1}{M_{N}} \sum_{i=1}^{M_{N}}\left[\tanh \left(\sum_{j=1}^{\pi_{i}^{-1}(k)} y_{\pi_{i}(j)}\right)-\tanh \left(\sum_{j=1}^{\pi_{i}^{-1}(k)-1} y_{\pi_{i}(j)}\right)\right] \tag{29}
\end{equation*}
$$

This linearization technique is an approximation to the Shapley Values.(?)

## Experiments: Stanford Sentiment Tree Bank

- Unigram Word Scores: Correlation with the logistic regression coefficient

| Attribution Method | Heat Map |
| :--- | :--- |
| Gradient | It's easy to love Robin Tunney - she's pretty and she can act - |
|  | but it gets harder and harder to understand her choices. |
| Leave one out (Li et al., <br> 2016) | It's easy to love Robin Tunney - she's pretty and she can act - |
|  | but it gets harder and harder to understand her choices. |
| Cell decomposition <br> (Murdoch \& Szlam, <br> 2017) | It's easy to love Robin Tunney - she's pretty and she can act - |
| Integrated <br> (Sundararajan <br> 2017) | gradients <br> et |
| Contextual <br> tion | It's easy to love Robin Tunney - she's pretty and she can act - |
|  | but it gets harder and harder to understand her choices. |
|  | It's easy to love Robin Tunney - she's pretty and she can act - |

Table 2: Heat maps for portion of review from SST with different attribution techniques. Only CD captures that the first phrase is positive.

## Identifying Dissenting Subphrases

- "used to be my favorite"
- favorite is positive, used to be is negative

| Attribution Method | Heat Map |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Gradient | used | to be | my | favorite | not | worth | the | time |
| Leave One Out (Li et al., 2016) | used | to be | my | favorite | not | worth | the | time |
| Cell decomposition (Murdoch \& Szlam, 2017) | used | to be | my | favorite | not | worth | the | time |
| Integrated gradients (Sundararajan et al., 2017) | used | to be | my | favorite | not | worth | the | time |
| Contextual decomposition | used | to be | my | favorite | not | worth | the | time |
| Legend Very Negative |  | Negative | Neutra | al Positive | Very Positive |  |  |  |

Table 1: Heat maps for portion of yelp review with different attribution techniques. Only CD captures that "favorite" is positive.

## Contextual Decomposition Captures Negation



Contextual Decomposition


Figure 1: Distribution of scores for positive and negative negation coefficients relative to all interaction coefficients. Only leave one out and CD are capable of producing these interaction scores.

## Identifying Similar Phrases

- Compare Dense embeddings $\beta_{T}$ average for phrases across the training set and validation set
- Get nearest neghbors

| not entertaining | not bad | very funny | entertaining | bad |
| :---: | :---: | :---: | :---: | :---: |
| not funny | never dull | well-puttogether piece | intelligent | dull |
| not engaging | n't drag | entertaining romp | engaging | drag |
| never satisfactory | never fails | very good | satisfying | awful |
| not well | without sham | surprisingly <br> sweet | admirable | tired |
| not fit | without missing | very wellwritten | funny | dreary |

Table 3: Nearest neighbours for selected unigrams and interactions using CD embeddings

